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# Undecidability of Coverability and Boundedness for Timed-Arc Petri Nets with Invariants

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**Abstract.** Timed-Arc Petri Nets (TAPN) is a well studied extension of the classical Petri net model where tokens are decorated with real numbers that represent their age. Unlike reachability, which is known to be undecidable for TAPN, boundedness and coverability remain decidable. The model is supported by a recent tool called TAPAAL which, among others, further extends TAPN with invariants on places in order to model urgency. The decidability of boundedness and coverability for this extended model has not yet been considered. We present a reduction from two-counter Minsky machines to TAPN with invariants to show that both the boundedness and coverability problems are undecidable.

## 1 Introduction

Time-dependent models have been extensively studied due to increasing demands on the reliability and safety of embedded software systems. *Timed automata* [11] and various time-extensions of *Petri nets* (e.g. [4]) are among the most studied time-dependent models. A recent paper by Srba [14] provides a comparative overview of these models.

*Timed-Arc Petri Nets* (TAPN's) [4] is a popular time-extension of Petri Nets [10] in which each token is assigned an age (a real number), and time intervals on arcs restrict the ages of tokens that can be used to fire a transition. The reachability problem has been shown undecidable for TAPN [12]. In particular, a TAPN cannot correctly simulate a test for zero on a counter [3]. However, other problems, like boundedness and coverability remain decidable [2][1].

Recent work on the verification tool TAPAAL by Byg et al. [5] have, among other things, introduced invariants on places into the TAPN model as a way to represent urgency. However, urgency alone does not allow a TAPN to correctly simulate a test for zero on a counter. Nevertheless, we show that invariants on places makes the coverability and boundedness problem undecidable. We adopt the main idea from [12] (see also [6] for a similar proof technique for another time extension of Petri nets), in which a two-counter Minsky machine (2-CM) is weakly simulated by a TAPN. In contrast to their reduction, the extension of invariants allows us to detect when the net incorrectly simulates the 2-CM. Further, our reduction allows us to prove the undecidability of both the coverability and boundedness problems.

## 2 Basic Definitions

Many of the definitions in this section are following [13]. The set of all *time intervals*  $\mathcal{I}$  and the set of time intervals for invariants  $\mathcal{I}_{Inv}$  are defined according to the following abstract syntaxes where  $a \in \mathbb{N}_0$ ,  $b \in \mathbb{N}$  and  $a < b$ :

$$\begin{aligned} I &::= [a, a] \mid [a, b] \mid [a, b) \mid (a, b] \mid (a, b) \mid [a, \infty) \mid (a, \infty) \\ I_{Inv} &::= [0, 0] \mid [0, b] \mid [0, b) \mid [0, \infty) \end{aligned}$$

We define the predicate  $r \in I$  for  $r \in \mathbb{R}_0^+$  in the expected way.

**Definition 1 (Timed-Arc Petri Net with Invariants).** A Timed-Arc Petri Net with Invariants (ITAPN) is a 5-tuple  $N = (P, T, F, c, \iota)$  where  $P$  is a finite set of places,  $T$  is a finite set of transitions such that  $P \cap T = \emptyset$ ,  $F \subseteq (P \times T) \cup (T \times P)$  is the flow relation,  $c : F|_{P \times T} \rightarrow \mathcal{I}$  is a function assigning time intervals to arcs from places to transitions, and  $\iota : P \rightarrow \mathcal{I}_{Inv}$  is a function assigning invariants to places.

We let  $\mathcal{B}(\mathbb{R}_0^+)$  denote the set of finite multisets over  $\mathbb{R}_0^+$ . For a  $B \in \mathcal{B}(\mathbb{R}_0^+)$  and some  $d \in \mathbb{R}_0^+$ , we let  $B + d = \{b + d \mid b \in B\}$ . Notationally, we use multisets as ordinary sets with the operations  $\cup, \setminus, \subseteq, \in$  implicitly interpreted over multisets.

Let us now define a marking on a ITAPN.

**Definition 2 (Marking).** A marking  $M$  on a ITAPN  $N = (P, T, F, c, \iota)$  is a function  $M : P \rightarrow \mathcal{B}(\mathbb{R}_0^+)$ , such that for every place  $p \in P$  it holds that for every token  $x \in M(p)$ ,  $x \in \iota(p)$ . The set of all markings over  $N$  is denoted  $\mathcal{M}(N)$ .

A *marked ITAPN* is a pair  $(N, M_0)$  where  $N$  is a ITAPN and  $M_0$  is the initial marking. We only allow initial markings in which all tokens have age 0.

The *preset* of a transition  $t$  is  $\bullet t = \{p \in P \mid (p, t) \in F\}$  and the *postset* of  $t$  is  $t^\bullet = \{p \in P \mid (t, p) \in F\}$ .

**Definition 3 (Firing rule).** Let  $N = (P, T, F, c, \iota)$  be a ITAPN,  $M$  some marking on it and  $t \in T$  be a transition of  $N$ .

We say that  $t$  is *enabled* if and only if  $\forall p \in \bullet t. \exists x \in M(p). x \in c(p, t)$ , i.e. there is a token with an appropriate age at every place in the preset of  $t$ .

If  $t$  is enabled in  $M$ , it can be fired, whereby we reach a marking  $M'$  defined by  $\forall p \in P. M'(p) = (M(p) \setminus C_t^-(p)) \cup C_t^+(p)$  (note that all operations are on multisets and there may be multiple choices for the sets  $C_t^-(p)$  and  $C_t^+(p)$  for each  $p$ . We simply fix the sets before firing  $t$ ), where

$$\begin{aligned} - C_t^-(p) &= \begin{cases} \{x\} & \text{if } p \in \bullet t \wedge x \in M(p) \wedge x \in c(p, t) \\ \emptyset & \text{otherwise} \end{cases} \\ - C_t^+(p) &= \begin{cases} \{0\} & \text{if } p \in t^\bullet \\ \emptyset & \text{otherwise} \end{cases} \end{aligned}$$

i.e. from each place  $p \in \bullet t$  we remove a token with an appropriate age, and we add a new token with age 0 to every  $p \in t^\bullet$ .

**Definition 4 (Time delays).** Let  $N = (P, T, F, c, \iota)$  be a ITAPN and  $M$  some marking on it. A time delay  $d \in \mathbb{R}_0^+$  is allowed if and only if  $(x + d) \in \iota(p)$  for all  $p \in P$  and  $x \in M(p)$ , i.e. by delaying  $d$  time units no token violates the invariants. By delaying  $d$  time units we reach a marking  $M'$ , defined as  $M'(p) = M(p) + d$  for all  $p \in P$ .

A marked ITAPN  $(N, M_0)$  is said to be *k-bounded* if the number of tokens in each place does not exceed  $k$  for any marking reachable from  $M_0$ . A marked ITAPN is *bounded* if it is *k-bounded* for some  $k \in \mathbb{N}$ .

*Problem 1 (Boundedness).* Given a marked ITAPN is it bounded?

A marking  $M$  on a ITAPN  $(N, M_0)$  is said to be *coverable* if there exists a marking  $M'$ , reachable from  $M_0$ , s.t.  $M'(p) \supseteq M(p)$  for each place  $p$  in the net.

*Problem 2 (Coverability).* Given a marked ITAPN  $(N, M_0)$  and some marking  $M$ , is  $M$  coverable?

### 3 Undecidability of Boundedness and Coverability

In this section we will prove the undecidability of boundedness and coverability by reduction from two-counter Minsky machines.

**Definition 5.** A Two-Counter Minsky Machine (2-CM) with two non-negative registers  $r_1$  and  $r_2$  is a sequence of instructions  $(I_1 : Ins_1; I_2 : Ins_2; \dots I_{e-1} : Ins_{e-1}; I_e : HALT)$  where for every  $j$ ,  $1 \leq j < e$ ,  $Ins_j$  is one of the two types:

- $r_i := r_i + 1$ ; **goto**  $I_k$ ; where  $i \in \{1, 2\}$  and  $k \in \{1, 2, \dots, e\}$  (Increment).
- if  $r_i > 0$  then  $r_i := r_i - 1$ ; **goto**  $I_k$ ; else **goto**  $I_\ell$ ; where  $i \in \{1, 2\}$  and  $k, \ell \in \{1, 2, \dots, e\}$  (Test and decrement).

The last instruction is always the HALT instruction. A configuration of a 2-CM is a triple  $(j, v_1, v_2)$  where  $j \in \{1, 2, \dots, e\}$  is the index of instruction  $I_j$  to be executed and  $v_1$  and  $v_2$  are the values of the registers  $r_1$  and  $r_2$ , respectively.

The computational step relation of a 2-CM is defined as expected and we use the notation  $(j, v_1, v_2) \rightarrow (j', v'_1, v'_2)$  to denote that we perform the current instruction  $I_j$  with values  $v_1$  and  $v_2$  in the registers, resulting in the configuration  $(j', v'_1, v'_2)$ .

**Definition 6 (The Halting Problem for 2-CM).** Given a 2-CM, is it possible to reach the halt instruction from the initial configuration  $(1, 0, 0)$ , i.e.  $(1, 0, 0) \rightarrow^* (e, v_1, v_2)$  for some  $v_1, v_2 \in \mathbb{N}_0$ ?

**Theorem 1 (Minsky [9]).** The halting problem for 2-CM is undecidable.

We will now describe the reduction from 2-CM to ITAPN. Given a 2-CM  $(I_1 : Ins_1; I_2 : Ins_2; \dots I_{e-1} : Ins_{e-1}; I_e : HALT)$  we construct a ITAPN  $(P, T, F, c, \iota)$  where

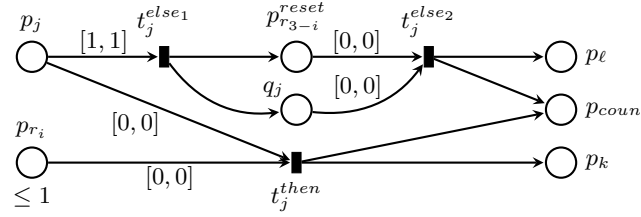
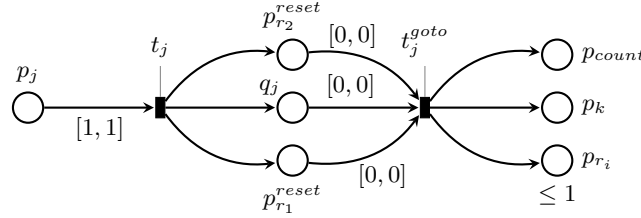
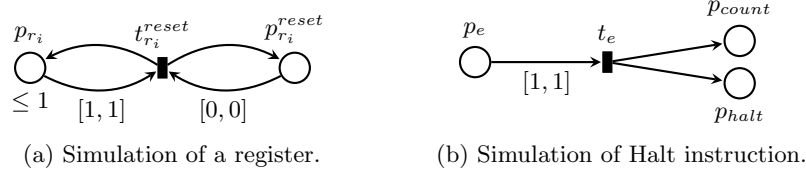


Fig. 1: ITAPN models for 2-CM simulation.

- $P = \{p_j, q_j \mid 1 \leq j < e\} \cup \{p_{r_1}, p_{r_1}^{reset}, p_{r_2}, p_{r_2}^{reset}\} \cup \{p_{count}\} \cup \{p_e, p_{halt}\}$
- $T = \{t_{r_1}^{reset}, t_{r_2}^{reset}\} \cup \{t_j, t_j^{goto} \mid Ins_j \text{ is of type increment}\} \cup \{t_j^{else1}, t_j^{else2}, t_j^{then} \mid Ins_j \text{ is of type test and decrement}\} \cup \{t_e\}$

The number of tokens in  $p_{r_1}$  and  $p_{r_2}$  correspond to the values of  $r_1$  and  $r_2$ , the number of tokens in  $p_{count}$  remembers the number of computation steps which have been simulated in the net and  $p_1, \dots, p_e$  corresponds to the instructions  $Ins_1, \dots, Ins_e$  such that the place  $p_j$  contains one token if and only if the current instruction is  $Ins_j$ . For the flow relation we will split it into 4 parts.

- $F_1$  contains the arcs for the registers. For each register  $r_i$ ,  $i \in \{1, 2\}$ , we add the following arcs to  $F_1$

$$(p_{r_i}, t_{r_i}^{reset}), (t_{r_i}^{reset}, p_{r_i}), (p_{r_i}^{reset}, t_{r_i}^{reset}), (t_{r_i}^{reset}, p_{r_i}^{reset}) \text{ where} \\ c((p_{r_i}, t_{r_i}^{reset})) = [1, 1], \quad c((p_{r_i}^{reset}, t_{r_i}^{reset})) = [0, 0] \text{ and } \iota(p_{r_i}) = [0, 1].$$

This is illustrated in Figure 1a. The number of tokens on  $p_{r_i}$  indicates the value of the register. Notice the invariant on the register which disallows tokens with an age greater than 1. Placing a token on  $p_{r_i}^{reset}$  allows us to reset the age of all tokens of age 1 in the register.

- $F_2$  contains the arcs for the increment instructions. For each increment instruction  $I_j : r_i := r_i + 1$ ; **goto**  $I_k$ ;, we add the following arcs to  $F_2$

$$(p_j, t_j), (t_j, p_{r_2}^{reset}), (t_j, q_j), (t_j, p_{r_1}^{reset}), (p_{r_2}^{reset}, t_j^{goto}), (q_j, t_j^{goto}), \\ (p_{r_1}^{reset}, t_j^{goto}), (t_j^{goto}, p_{count}), (t_j^{goto}, p_k), (t_j^{goto}, p_{r_i}) \text{ where } c((p_j, t_j)) = [1, 1], \\ c((p_{r_2}^{reset}, t_j^{goto})) = [0, 0], \quad c((q_j, t_j^{goto})) = [0, 0] \text{ and } c((p_{r_1}^{reset}, t_j^{goto})) = [0, 0].$$

This is illustrated in Figure 1c. Notice that we require a delay of one time unit before firing  $t_j$ . Because of this, we allow tokens in each register to be reset (by placing tokens on  $p_{r_1}^{reset}$  and  $p_{r_2}^{reset}$ ). Following this, by firing  $t_j^{goto}$  a token is added to  $p_{count}$ , register  $r_i$  is incremented by adding a token to  $p_{r_i}$  and control is given to the next instruction  $I_k$  by placing a token on  $p_k$ .

- $F_3$  contains the arcs for the test and decrement instructions. For each test and decrement instruction  $I_j$  : if  $r_i > 0$  then  $r_i := r_i - 1$ ; **goto**  $I_k$ ; **else goto**  $I_\ell$ ;, we add the following arcs to  $F_3$

$$(p_j, t_j^{else1}), (p_j, t_j^{then}), (p_{r_i}, t_j^{then}), (t_j^{else1}, q_j), (t_j^{else1}, p_{r_{3-i}}^{reset}), (q_j, t_j^{else2}), \\ (p_{r_{3-i}}^{reset}, t_j^{else2}), (t_j^{else2}, p_\ell), (t_j^{else2}, p_{count}), (t_j^{then}, p_{count}), (t_j^{then}, p_k) \text{ where} \\ c((p_j, t_j^{else1})) = [1, 1], \quad c((p_j, t_j^{then})) = [0, 0], \quad c((p_{r_i}, t_j^{then})) = [0, 0], \\ c((p_{r_{3-i}}^{reset}, t_j^{else2})) = [0, 0] \text{ and } c((q_j, t_j^{else2})) = [0, 0].$$

This is illustrated in Figure 1d. Notice that when we follow the else branch (firing transition  $t_j^{else1}$ ), we can only reset the ages of tokens in the register on which we are not testing for emptyness.

- $F_4$  contains the arcs for the HALT instruction. Formally it is defined as

$$F_4 = \{(p_e, t_e), (t_e, p_{count}), (t_e, p_{halt})\} \text{ where } c((p_e, t_e)) = [1, 1].$$

This is illustrated in Figure 1b. Again we require a time delay of one time unit before  $t_e$  can be fired and a token placed at  $p_{halt}$ .

- The flow relation  $F$  can then be defined as the union of the four parts, i.e.  $F = F_1 \cup F_2 \cup F_3 \cup F_4$  and we let  $\iota(p) = [0, \infty)$  for all  $p \in P \setminus \{p_{r_1}, p_{r_2}\}$ .

We define the initial marking  $M_0$  such that  $M_0(p_1) = \{0\}$  and  $M_0(p) = \emptyset$  for all  $p \in P \setminus \{p_1\}$ .

Let  $(N, M_0)$  be the marked ITAPN simulating a given 2-CM. Notice that every place in the net except for  $p_{r_1}, p_{r_2}, p_{count}$  is *1-safe* (i.e. contains at most one token). In a *correct* simulation of the 2-CM by our net, a configuration  $(j, v_1, v_2)$  of the 2-CM corresponds to any marking  $M$  where

$$M(p_j) = \{0\}, \quad M(p_{r_i}) = \underbrace{\{0, 0, \dots, 0\}}_{v_i \text{ times}} \text{ for } i \in \{1, 2\}, \quad (1)$$

$$|M(p_{count})| = n \text{ where } n \in \mathbb{N}_0 \text{ and } M(p) = \emptyset \text{ for all } p \in P \setminus \{p_j, p_{r_1}, p_{r_2}, p_{count}\}.$$

We will now describe how to simulate the three types of instructions of a 2-CM in a *correct* way. Assume there is a token of age 0 in  $p_j$ .

If  $I_j$  is an increment instruction, we need to delay for one time unit in order to enable  $t_j$  (see Figure 1c). Because we delayed one time unit, all tokens in the registers are now of age 1. In a correct simulation, we fire repeatedly transitions  $t_{r_1}^{reset}$  and  $t_{r_2}^{reset}$  until all tokens in  $p_{r_1}$  and  $p_{r_2}$  are of age 0. Note that it is possible to *cheat* in the simulation, as it is possible to leave some tokens of age 1 in  $p_{r_1}$  or  $p_{r_2}$  when firing  $t_j^{goto}$ .

If  $I_j$  is a test and decrement instruction there are two possibilities (see Figure 1d). If there is a token of age 0 at  $p_{r_i}$ , we fire  $t_j^{then}$  in order to decrement the number of tokens in register  $r_i$ , and hand over the control to  $I_k$  by placing a token on  $p_k$ . Otherwise, in the correct simulation we delay one time unit before firing  $t_j^{else1}$ . Then we reset the age of all the tokens in the other register,  $p_{r_{3-i}}$  to 0. We then proceed by firing  $t_j^{else2}$ . This will hand over control to instruction  $I_\ell$  by placing a token on  $p_\ell$ . Again note that it is possible to *cheat* in the simulation, either by leaving tokens of age 1 at  $p_{r_{3-i}}$  when proceeding to the next instruction or by taking the *else*-branch even though there is a token at  $p_{r_i}$  (because the net does not force us to fire transition  $t_j^{then}$  when it is enabled).

If  $I_j$  is the halt instruction, we delay one time unit before we fire the last transition  $t_e$  and add a token to  $p_{halt}$ .

After every instruction one token is added to  $p_{count}$ . We will now prove a lemma detailing what happens if we cheat.

**Lemma 1.** *Let  $(j, v_1, v_2)$  be the current configuration of a 2-CM CM,  $(N, M_0)$  the associated ITAPN and  $M$  a marking corresponding to  $(j, v_1, v_2)$  (see Equation 1). If the net cheats then during the simulation of CM in the next computation step it is not possible to simulate an increment instruction, go to the halt state, nor to take the else-branch of a test and decrement instruction. Further, the net can do at most  $v_1 + v_2$  decrements before getting stuck.*

*Proof.* We can perform an incorrect simulation in two ways:

- If all tokens in  $p_{r_1}$  and  $p_{r_2}$  are not reset to age 0 in an increment or test and decrement instruction before going to the next instruction.
- In a test and decrement instruction, the net can fire the transition  $t_j^{else1}$  even if there is a token of age 0 in  $p_{r_i}$ . This is possible by delaying 1 time unit to enable the transition. However, this will result in the tokens in  $p_{r_i}$  having age 1 and these can not be reset before going to the next instruction.

In both cases we end up in a marking  $M'$  where there is at least one token of non-zero age in either  $p_{r_1}$  or  $p_{r_2}$ . Observe that the simulation of increment, halt and the else-branch of a test and decrement instruction all require a delay of 1 time unit (see Figure 1) which would violate the invariants  $\iota(p_{r_1})$  or  $\iota(p_{r_2})$ . Thus, the only possibility is to take the then-branch of a test and decrement instruction. However, this is only possible as long as there are tokens of age 0 in  $p_{r_1}$  or  $p_{r_2}$ . There are  $v_1$  and  $v_2$  tokens in  $p_{r_1}$  and  $p_{r_2}$ , respectively. Thus, the net can do at most  $v_1 + v_2$  decrements before getting stuck.  $\square$

### 3.1 Undecidability Results

First we prove the undecidability of the boundedness problem.

**Lemma 2.** *Given a 2-CM CM and the associated ITAPN  $(N, M_0)$ , CM halts if and only if  $N$  is bounded.*

*Proof.* We start by proving that if  $N$  is bounded then CM halts. Assume that  $N$  is  $k$ -bounded. Further, assume by contradiction that CM does not halt. After simulating  $k+1$  computational steps of CM correctly, the net will be in a marking  $M$  where  $|M(p_{count})| = k+1$ . This is a contradiction to the assumption that  $N$  is  $k$ -bounded.

Now we prove the implication in the other direction. Assume that CM halts in  $n$  steps. We will show that  $N$  is  $2n$ -bounded. If we simulate CM correctly, there will be at most  $n$  tokens at the registers, and exactly  $n$  tokens at  $p_{count}$ . Hence, the net must cheat in order to become unbounded. In the worst case, it cheats at the last step, when there are at most  $n-1$  tokens in the registers and  $n-1$  tokens at  $p_{count}$ . Then we have that the net is  $2n$ -bounded since there will be at most  $2(n-1)$  tokens at  $p_{count}$  by Lemma 1.  $\square$

From Lemma 2 we conclude the following theorem.

**Theorem 2.** *The boundedness problem is undecidable for ITAPN.*

We now prove the undecidability of the coverability problem.

**Lemma 3.** *Let  $M$  be a marking such that  $M(p_{halt}) = \{0\}$  and  $M(p) = \emptyset$  for all  $p \in P \setminus \{p_{halt}\}$ . Given a 2-CM CM and the associated marked ITAPN  $(N, M_0)$ , as defined above, CM halts if and only if  $M$  is coverable from  $M_0$ .*

*Proof.* First we prove that if CM halts then  $M$  is coverable from  $M_0$ . Assume that the CM halts. By simulating CM correctly in  $N$ , we can easily see that we reach a marking  $M'$ , with a token in  $p_{halt}$ , hence  $M'(p) \supseteq M(p)$  for all  $p \in P$ .

Now we prove that if  $M$  is coverable from  $M_0$  then CM halts. Assume that  $M$  is coverable from  $M_0$ . By assumption there exists a reachable marking  $M'$  such that  $M'(p) \supseteq M(p)$  for all  $p \in P$ . By definition of coverability, it holds that  $0 \in M'(p_{halt})$  and by Lemma 1 this is only possible if we simulate CM correctly in the net, hence CM halts.  $\square$

From Lemma 3 we conclude the following theorem.

**Theorem 3.** *The coverability problem is undecidable for ITAPN.*

## 4 Conclusion

We proved that coverability and boundedness is undecidable for Time-Arcs Petri Nets with Invariants by reduction from two-counter Minsky machines. The following table shows a summary of known results about Petri Nets (PN). Our results are emphasized.



	Reachability	Boundedness	Coverability
PN	decidable [8]	decidable [7]	decidable [7]
TAPN	undecidable [12]	decidable [2]	decidable [1]
ITAPN	undecidable [12]	<i>undecidable</i>	<i>undecidable</i>

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